

Date 30/01/2020

class - XIIth

Subject - Mathematics

Ex 3.4 (N.C.E.R.T.)

Q.13 Find A^{-1} if $A = \begin{bmatrix} 2 & -3 \\ -1 & 2 \end{bmatrix}$

Solution, Given

$$A = \begin{bmatrix} 2 & -3 \\ -1 & 2 \end{bmatrix}$$

We write

$$A = IA$$

$$\Rightarrow \begin{bmatrix} 2 & -3 \\ -1 & 2 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} A$$

Applying $R_1 \rightarrow R_1 + R_2$, we get

$$\Rightarrow \begin{bmatrix} 2+(-1) & -3+2 \\ -1 & 2 \end{bmatrix} = \begin{bmatrix} 1+0 & 0+1 \\ 0 & 1 \end{bmatrix} A$$

$$\Rightarrow \begin{bmatrix} 1 & -1 \\ -1 & 2 \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix} A$$

$$\Rightarrow \begin{bmatrix} 1 & -1 \\ -1+1 & 2+(-1) \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ 0+1 & 1+1 \end{bmatrix} A$$

Applying
 $R_2 \rightarrow R_2 + R_1$

$$\Rightarrow \begin{bmatrix} 1 & -1 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ 1 & 2 \end{bmatrix} A$$

Applying $R_1 \rightarrow R_1 + R_2$, we

$$\begin{bmatrix} 1+0 & -1+1 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 1+1 & 1+2 \\ 1 & 2 \end{bmatrix} A$$

$$\Rightarrow \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 2 & 3 \\ 1 & 2 \end{bmatrix} A \quad \text{①}$$

Now comparing ① with

$$I = \bar{A}^{-1} A \quad \text{②, we get}$$

$$\bar{A}^{-1} = \begin{bmatrix} 2 & 3 \\ 1 & 2 \end{bmatrix} \text{ Ans}$$

Q. (8) Matrices A and B will be inverse of each other if

① $AB = BA$ ② $AB = BA = 0$ ③ $AB = 0, BA = 1$

& ④ $AB = BA = I$

Solution: we know that product of matrices & its reverse is a unit matrix.

$$\therefore AB = BA = I$$

So ④ is correct

— x — y —

chapter End